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SPACE SYSTEMS

DEFENSE SYSTEMS DEPARTMENT . SANTA BARBARA, CALIFORNIA



COMMUNICATION SYSTEMS ANALYSIS FOR LIGHTWEIGHT ROVING LUNAR VEHICLE

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61 SPC-4

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2,3 (1/V)

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INTRODUCTION

This TIS summarizes the results of the analysis carried out in three separate reports contained herein. The three reports are entitled "Communication Requirements" Nos. 1 through 3 respectively and are reproduced in this TIS in their original form.

All three reports analyze transmitter power requirements in terms of data rate for the same system parameters. The system parameters were obtained from a scrutiny of JPL Research Summaries, listed in the references throughout the report.

CONCLUSIONS

Reference to figure 1 of report #1, figure 2 of report #2 and figure 3 of report #3 indicates that transmitter powers of 15, 16, and 5.5 watts respectively are required for the same data rate. These results are tabulated below for ease of comparison. The results are based on the utilization of a 85° receiving antenna.

Table A

Minimum Transmitter Power
Requirements
85' Receiving Antenna

Modulation System	Data Rate	Transmi Watts	tter Power dbw
FM	5xl0 ⁵ elements per/sec(= 1:5xl0 ⁶ bits/sec)	5, 5	7.4
PCM - PS	1.5x10 ⁶ bits/sec	15	11.75
PCM - FM	1.5x10 ⁶ bits/sec	16	12

Where the analysis was based on the utilization of a 250[†]
DSIF receiving antenna, the minimum transmitter power requirements for each of the three modulation schemes are tabulated below.

Table B

Minimum Transmitter Power Requirements
250' Receiving Antenna

Modulation		Transmitter	Power
Scheme	Data Rate	Milliwatts	dbm
FM	5x10 ⁵ elements/sec (g 1.5x10 ⁵ bits/sec)	370	25.7
PCM - FM PCM - PS	1.5x10 ⁶ bits/sec 1.5x10 ⁶ bits/sec	940 1000	29. 75 30

COMMUNICATION REQUIREMENTS

REPORT # 1

PCM - PS

Preliminary Transmitter R. F. Power Requirements

The purpose of this report is to determine the transmitter power requirements as a function of data transmission rate for the Prospector moon-to-earth TV link.

The analysis that follows is based on the utilization of PCM-PS modulation at an r.f. carrier frequency of 2250 mc.

The ground based receiver station will utilize the DSIF equipment.

The transmitter power requirements utilizing FM and PCM-FM will be made the subject of later reports.

Video Input

The video input will be obtained from the output terminals of an image orthicon camera located aboard the "tank". The maximum data rate assumed is 1.5×10^6 bits/sec, i.e., 1000 vertical lines, 500 horizontal lines and 8 levels of grey,

Video Output

The video output from the communications system will consist of a train of binary pulses that will have a digit error of l in 10^5 .

System Parameters

Path distance moon-to-earth 2.5 x 10^5 statute miles

Carrier frequency 2250 mc.

Noise temperature T_g of moon (Ref. 1) 130°K

Diameter of receiving antenna (Ref. 2) 65 ft.

50 db
50°K
0.4 db
30°K
4 ft.
27 db
0.6 db
3 db

Analysis

The system noise temperature T_s of the receiving system

$$T_s = \begin{bmatrix} T_g + T_r \end{bmatrix} + \begin{bmatrix} L_r - 1 \end{bmatrix} T_o + \begin{bmatrix} T_e & L_r \end{bmatrix}$$
 (1) where $T_o = 290^{\circ}$ K

Hence, we obtain Ta

$$= [130 + 50] + [1.1 - 1] 290 + [30 \times 1.1]$$

$$= 242^{\circ} \text{ K}$$

The noise power Pn per cycle of post detection bandwidth is

$$P_n = 2KT_s = 1.38 \times 10^{-23} \times 2.42 \times 10^2 \times 2$$

= 6.68 x 10⁻²¹ watts/cps
= -202 dbw (2)

For a digit error of 10^{-5} we require a post detection S/N of 13 db (Ref. 5). The post detection bandwidth here is assumed to be equal to the data rate. If we let this bandwidth be B_n , then the noise power will be $P_{Bn} = 2 \text{ KT}_8 B_n$ watts (3). Then for a data rate of 1.5 x 10^6 bits/sec, we obtain from (2) and (3).

$$P_{Bn} = -202 + 10 \log_{10} 1.5 \times 10^6$$

= -140.25 dbw

Since there is no modulation gain in a PCM-PS system, then the received signal input power P_r , required for a 13 db output S/N is

$$P_r = P_{Bn} + 13 \text{ db}$$
 (4)
= -140.25 + 13 = -127.25 dbw

The received signal input power Pr is given by

$$P_r = P_t - L_t + G_t - C_t + G_r - L_r - L_p$$
 (5)

Where Pt is transmitter power level (ref to 1 watt)

Ci is the free space loss between isotropic antennas and is given by

$$\alpha = 37 + 20 \log f (mc) + 20 \log d (miles)$$

for f = 2250 mc and $d = 2.5 \times 10^5$ miles

we obtain $\alpha = 212$ db

The transmitter power required Pt is from (5)

$$P_t = P_r + L_t + CC + L_r + L_p - G_t - G_r$$

and for the 1.5 x 106 bit/sec data we get

$$P_t = -127.25 + 0.6 + 212 + 0.4 + 3 - 27 - 50$$

= 11.75 dbw = 15 watts

Values of P_t required for data rates between 5 x 10⁴ and 1.5 x 10⁶ bits/sec are tabulated in Table 1. The results of Table 1 are plotted in Figure 1.

Gase for 250 Foot Antenna at DSIF

If the 250'dish is utilized at the DSIF site, the system parameters are changed as follows: (Ref. 2)

Receiving antenna gain G_r increased to 61 db.

Receiving antenna noise temperature Ta, reduced to 150 K.

The system noise temperature T_a , is reduced by 35° K to 242-35 = 207° K and the thermal noise power per cycle of bandwidth is reduced from -202 dbw to -202 - 10 log $\frac{242}{217}$ = 202.7 dbw.

The noise N_{Bn} in a 1.5 mc bandwidth becomes -(140.25 + 0.7) = say -141 dbw and the received signal power required, $P_r = -141 + 13 = -128$ dbw.

The system transmission gain, however, is increased by 11 db due to the higher receiving antenna gain. The net result is that the transmitter power requirements are reduced by 11 + 0.7 = 11.7 db.

Transmitter power requirements as a function of data rate utilizing the 250 ft. DSIF antenna, are tabulated in Table II.

The results of Table II are plotted in Figure 2.

References

- 1. G. E. Co., DED presentation "Techniques Applicable to Lunar Landing", Feb. 10, 1960. Page 27, Chart 6-1
- 2. JPL Technical Memo 33-27, Feb. 13, 1961. Page 22
- 3. JPL Research Summary 36-7, Vol. 1, Feb. 15, 1961.
 Page 78
- 4. H. I. Ewen, "A Thermodynamic Analysis of Maser Systems", Microwave J, Vol. 2, Pages 41-46, March 1959.
- 5. H. N. Putschi, "Evaluation and Development of a PCM-PS Radio Telemetry System". G. E. Co., TIS R59ELS34, May 7, 1959. Figure 16
- 6. Reference Data for Radio Engineers, LTTL, 4th edition. Page 751

Table I

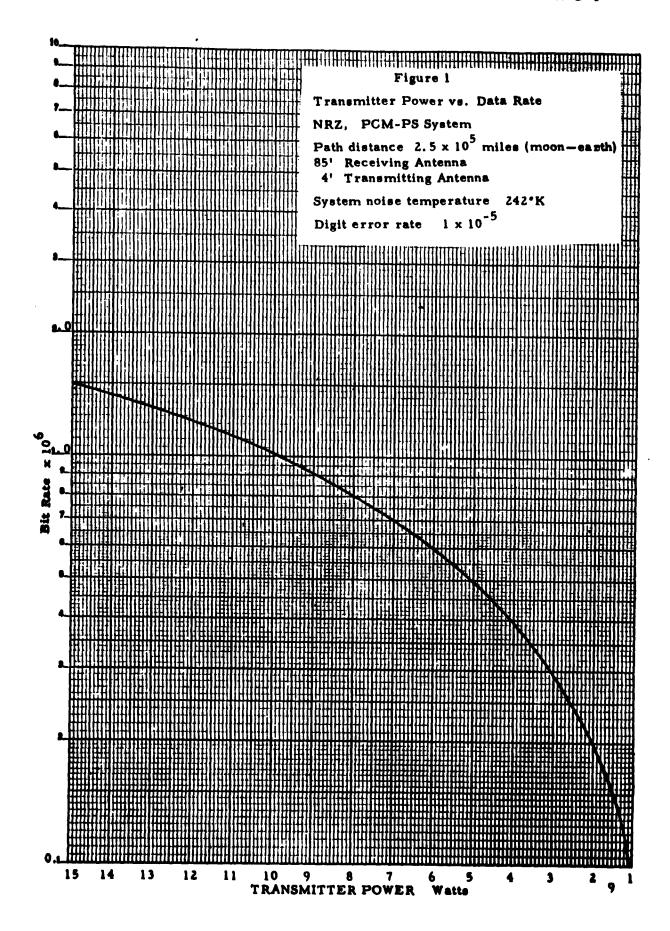
Transmitter Power Vs. Data Rate, 85 ft. Antenna

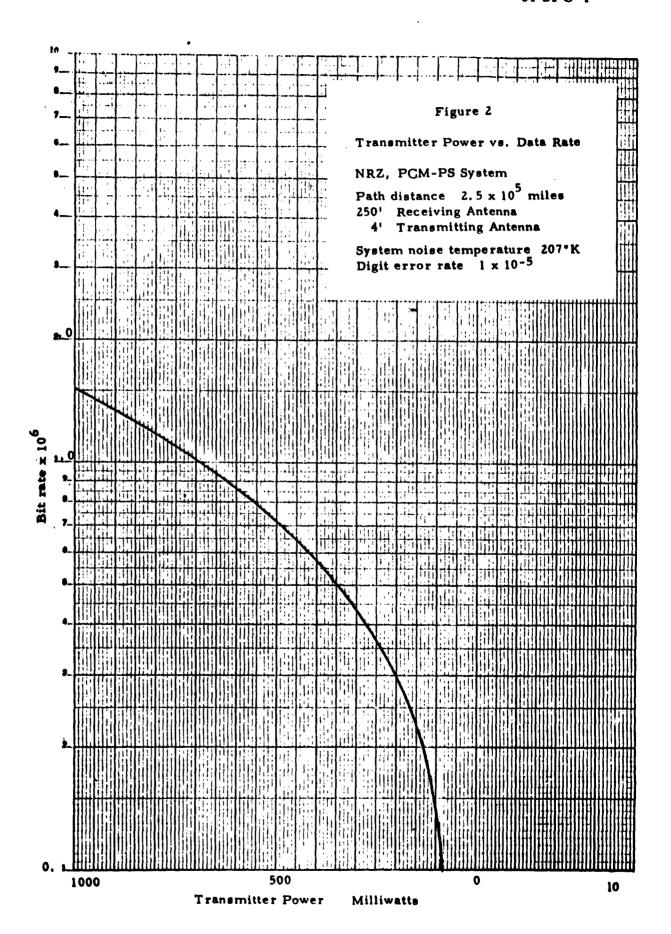
Data Rate, bits/sec	Noise Band- width, Bn	Noise Band- Noise Power width, B _n P _{Bn} in B _n (dbw)	Output S/N Rec'l. for Re= 10-5 (db) power Pr(dbw	Rec'l. signal power Pr(dbw)	Net Trans- Trans- mission mitter loss N _L power (db) P _t (dbw)		P _t Watts
1.5 × 10 ⁶	1.5 mc	-140.25	13	-127.25	-139	11.75	15
1.0 × 106	1 mc	-142	13	-129	-139	10	10
5×10^5	500 kc	-145	13	-132	-139	7	Ŋ
2.5 x 10 ⁵	250 kc	-148	13	-135	-139	4	2.5
1 × 10 ⁵	100 kc	-152	13 ·	-139	-139	0	1.0
5 x 104	50 kc	-155	13	-142	-139	-3	0.5

Table II

Transmitter Power Vs. Data Rate, 250 ft. Antenna

Data Rate Noise bits / sec width,	Noise Band- width, Bn	Band- Noise Power Bn PBn (dbw)	O/P S/N for R = 10-5 (db)	Rec'd. signal power Pr(dbw)	Net trans- mission loss (db)	Trans	Transmitter Power bw dbm milli watts	Power milli-
1.5 × 10 ⁶	1.5 mc	-141	13	-128	821-	0	30	1000
1.0×10^6	1 mc	-142.7	13	-129.7	-128	-1.7	-1.7 28.3	663
5 x 10 ⁵	500 kc	-145.7	13	-132.7	-128	4.7	4.7 25.3	340
2.5×10^5	250 kc	-148.7	13	-135.7	-128	-7.7	-7.7 22.3	170
1 × 10 ⁵	100 kc	-152.7	13	-139.7	-128	-11.7 18.3	18.3	89
5 × 104	50 kc	-155.7	13	-142.7	-128	-14.7 15.3	15.3	34
					•			





COMMUNICATION REQUIREMENTS

REPORT #2 PCM - FM

Preliminary Transmitter RF Power Requirements

This report discusses the transmitter power requirements as a function of data rate for the Prospector moon-earth T. V. link.

The analysis that follows is based on the utilization of a PCM-FM modulation system at a carrier frequency of 2250 mc.

The ground based receiver station will utilize DSIF equipment.

System Parameters

Path distance moon-earth 2, 5 x 10 ⁵ state	ute miles
Carrier frequency - 2250 mc	
Noise temperature Tg of moon (1)	130° K
Gain of 85' receiving antenna (2) G _r	50 db
Noise temperature, T _r of 85' receiving	
antenna (2)	50° K
Gain of 250' receiving antenna, (2) Gr	61 db
Noise temperature T _r of 250' receiving	
antenna ⁽²⁾	15° K
Receiving antenna feed and coupling	
losses, L _r (2)	0, 4 db
Circular polarization losses, Lp	3 db
Gain of 4' diameter transmitting	
antenna, Gr	27 db

Transmitting antenna coupling and other

0.6 db

Maser amplifier effective temperature, (3)

30° K

Analysis

The system noise temperature T_s is given by ⁽⁴⁾

$$T_{o} = \begin{bmatrix} T_{g} + T_{r} \end{bmatrix} + \begin{bmatrix} L_{r} - 1 \end{bmatrix} T_{o} + \begin{bmatrix} T_{e}L_{r} \end{bmatrix}$$

$$T_{o} = 290 \cdot K$$
(1)

where

and for the 85' antenna system we obtain

$$T_a = 242^{\circ} K$$

For the 250' antenna system we get $T_8 = 207^{\circ} \text{ K}$.

The thermal noise P_n in the I.F. bandwidth, B_{IF} is

$$P_n = KT_8 B_{IF}$$
 (2)
= 1.38 x 10⁻²³ $T_8 B_{IF}$

for the 85' antenna system we get

 $P_n = 3.34 \times 10^{-21}$ watts/cycle = -205 dbw/cps

and for the 250' antenna system we get

$$P_n = -205.7 \text{ dbw/cps}$$

The post detection output S/N of a FM system is given by (See Appendix I)

$$S/N_{db} = 10 \log_{10} \frac{P_R}{P_n} + 10 \log_{10} (\frac{B_{IF}}{2 B_V}) + 20 \log_{10} (\frac{\Delta F}{f_m}) +$$

Where P, is the received signal power

P_n is the thermal noise power in the I.F. bandwidth

BIF is the I. F. bandwidth

By is the post detection bandwidth

A r is the peak deviation of the r.f. carrier

 $f_{\rm m}$ is the highest modulating frequency (= B_V)

The +5 db term is the triangular noise spectrum improvement factor, characteristic of a F. M. discriminator.

The -3 db term is the efficiency correction factor for imperfect limiting.

The ratio $(\frac{\Delta F}{f m})$ is the modulation index of the system.

F.M. Improvement Threshold

Equation (3) is only valid provided that the signal level in the I.F. amplifier is above the improvement threshold of the receiver. The improvement threshold is defined as the signal level where the peak signal is equal to or greater than the peak noise. Since the input noise is assumed to be "white noise" it has a Gaussian distribution. Reference to Figure 1 shows that for 99.9% of the time the peak to RMS voltage factor does not exceed approximately 10 db. We therefore define the improvement threshold as the "10 db threshold". The received signal power required

$$P_{R}$$
 , . = $P_{n} + 10 \text{ db}$ (4)

I.F. Bandwidth

The I.F. bandwidth, B_{IF}, is given by ⁽⁵⁾

$$B_{IF} = 2 \left(\Delta F + B_{v} \right) \tag{5}$$

Equation (5) states that the I.F. bandwidth required is twice the sum

of the peak deviation and the video bandwidth. It should be noted that doppler shift and frequency drift is neglected.

Video Bandwidth

In order to make a fair comparison between the PCM-PS system discussed in Report #1 and a PCM-FM system we will assume that the video bandwidth $B_{\rm V}$ for the FM case is the same as for the PS case, i.e., $B_{\rm V}$ equal to the data rate.

Transmitter power V_S data rate is tabulated in Tab'es I and II for modulation indices of 1 and 2.4 respectively utilizing 85' receiving antennas. Tables III and IV indicate transmitter power requirements utilizing 250' receiving antennas.

The results of Tables I through IV are plotted in Figures 2 - 5 respectively.

References

- (1) G. E., D. E.D. Presentation "Techniques Applicable to a Lunar Landing", February 19, 1960, page 27, Chart 6-1.
- (2) J. P. L. Technical Memorandum 33-27, February 13, 1961, page 22.
- (3) J. P. L. Research Summary 36-7, Volume I, February 15, 1961, page 78.
- (4) H. I. Ewen, "A Thermodynamic Analysis of Maser Systems"

 Microwave J., Volume 3, March 1959, pages 41 46.
- (5) H. S. Black, "Modulation Theory" D. Van Nostrand Co.,
 November 1958, pages 200 202.

TABLE I

TRANSMITTER POWER VS DATA RATE

PCM-FM 85' RECEIVING ANTENNA

Modulation Index of 1

Data Rate	Video Band-	Peak De - viation	IF Band- width (= 2(\DF + B_v))	Noise Power in Bif. Pn I. F. (dbw)	Received Signal Power PR (dbw)	Net Trans- mission Loss (db)	Transmitter Power dbw Wal	tter Watts	O/P S/N (db)
bits/sec	widtn							•	ŭ
901	, 1	1. 5 mc	6 mc	- 137	- 127	139	12	91	C C
1.5 × 10 ·	₹	•		1 39	- 129	139	01	.10	15
1.0×10^{6}	n ac) mc	1				•	u	1.5
501	500 kc	500 kc	2.mc	- 142	- 132	139	-	n	:
) X C	}			145	- 135	139	*	2.5	15
2.5×10^{5}	250 kc	250 kc	T EBC		! !		c	-	15
1 × 105	100 kc	100 kc	400 kc	- 149	- 139	139	•	•	•
5 x 104	3	.50 kc	200 kc	- 152	- 142	139	۳	0.5	J.

Probability of error, Pe. < 10-7

TABLE II
TRANSMITTER POWER VS DATA RATE
PCM.-FM 85' RECEIVING ANTENNA
Modulation Index of 2.4

tter Output S/N Watts (db)	25 25	16 25	8 25	4 25	1.6 25	0.8 25
Transmi Power dbw	14	12	6	•	7	-1
Net Trans- mission Loss (db)	139	139	139	139	139	139
Received Signal Power (dbw)	- 125	- 127	- 130	- 133	- 137	- 140
Noise Power in B _{if} (dbw)	- 135	- 137	- 140	- 143	- 147	- 150
I. F. Band- width Bif	10.2 mc	6.8 mc	3.4 mc	1.7 mc	680 kc	340 kc
△F Peak Deviation	3.6 mc	2. 4 mc	1.2 mc	600 kc	240 kc	120 kc
Video Band- width B _v	1.5 mc	1 mc	500 kc	250 kc	100 kc	50 kc
Data Rate bits/sec	1.5 x 10 ⁶ 1.5 mc	1.0 × 10 ⁶	5 x 10 ⁵	2.5×10^5	1 × 105	5 x 104

 $P_{\bullet} << 10^{-7}$

 $P_{\bullet} < 10^{-7}$

TABLE III

TRANSMITTER POWER VS DATA RATE PCM-FM, 250' RECEIVING ANTENNA

Modulation Index of 1

						91	2
9	15	15	15	15	15	15	
(milli - watts)	940	670	335	168	29	33.5	
(dpm)	29.75	28. 25	25. 25	22. 25	18. 25	15.25	
(mqp)	0.25	-1.75	4.75	-7.75	-11.75	-14.75	
(qp)	128	1 28	1 28	128	128	128	
(dbw)	- 127.75	- 129.75	- 132.75	- 135.75	- 139.75	- 142.75	
(dpw)	-137.73	-139.75	,-142.75	-145.75	-149.75	-152.75	
B _{if}	6 mc	4 mc	2 mc	1 mc	400 kc	200 kc	
DF	1.5 mc	1 mc	500 kc	250 kc	100 kc	50 kc	
B	1.5 mc	1 mc	500 kc	250 kc	100 kc	50 kc	
bits/sec	1.5 x 10 ⁶	1.0 × 10 ⁶	5 × 10 ⁵	2.5×10^5	1.0×10^5	5 x 104	
	$\mathbf{B_v}$ $\Delta \mathbf{F}$ $\mathbf{B_{if}}$ (dbw) (dbw) (dbw) (dbm)	sec B _V	sec B _v	sec B _V \(\text{A} \text{F} \) B _{\text{if} \) (db\(w\)) (db\(w\)) (db\(w\)) (db\(w\)) (db\(w\)) (millingler) (db\(w\)) (db\(w\)) (db\(w\)) (millingler) (106 1.5 mc 1.5 mc 6 mc -137.73 -127.75 128 0.25 29.75 940 c106 1 mc 1 mc 4 mc -139.75 -129.75 128 -1.75 28.25 670 c105 500 kc 2 mc \(\frac{1}{2}\text{142.75} -132.75 \) 128 \(\frac{1}{4}\text{12}\text{75} \) 25.25 335}	sec By	sec By	sec By \(\text{D}\text{F}\) \(\text{B}\text{I}\text{J}\) \(\text{d}\text{B}\text{W}\) \(\text{d}\text{B}\text{W}\) \(\text{d}\text{B}\text{W}\) \(\text{d}\text{B}\text{M}\) \(\text{d}\text{B}\text{M}\text{M}\) \(\text{d}\text{B}\text{M}

TABLE IV

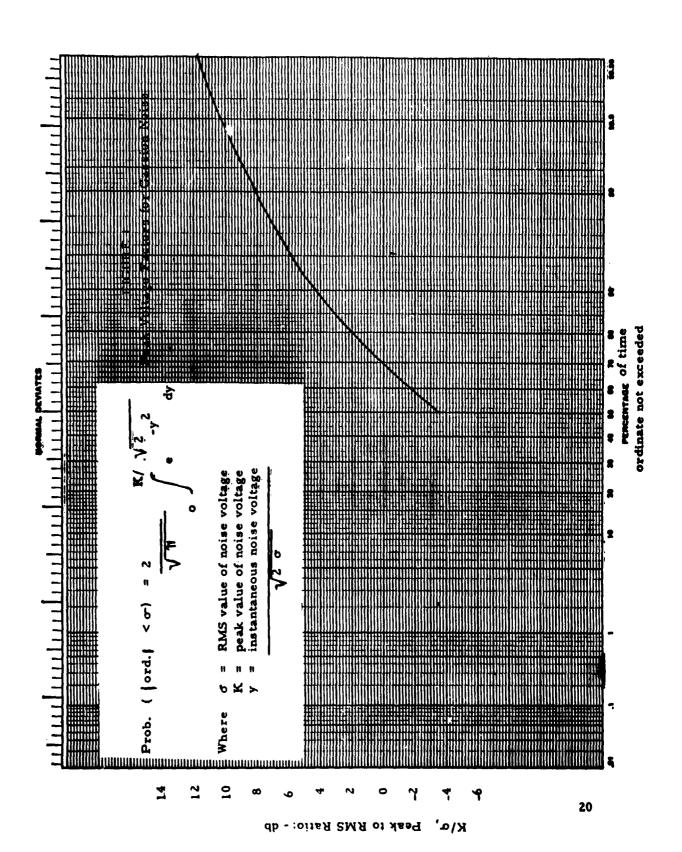
TRANSMITTER POWER VS DATA RATE

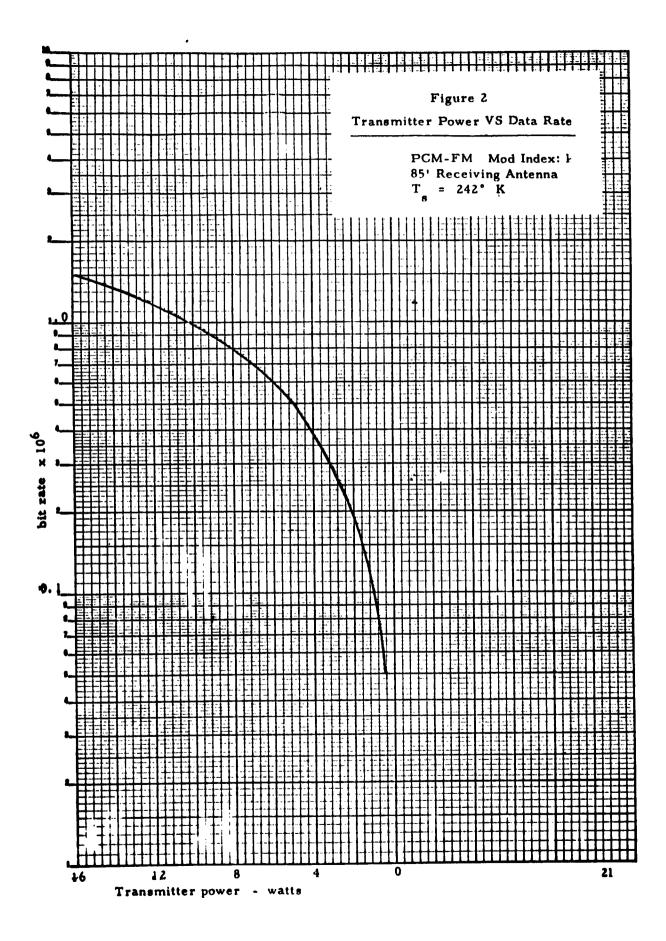
PCM-FM, 250' RECEIVING ANTENNA

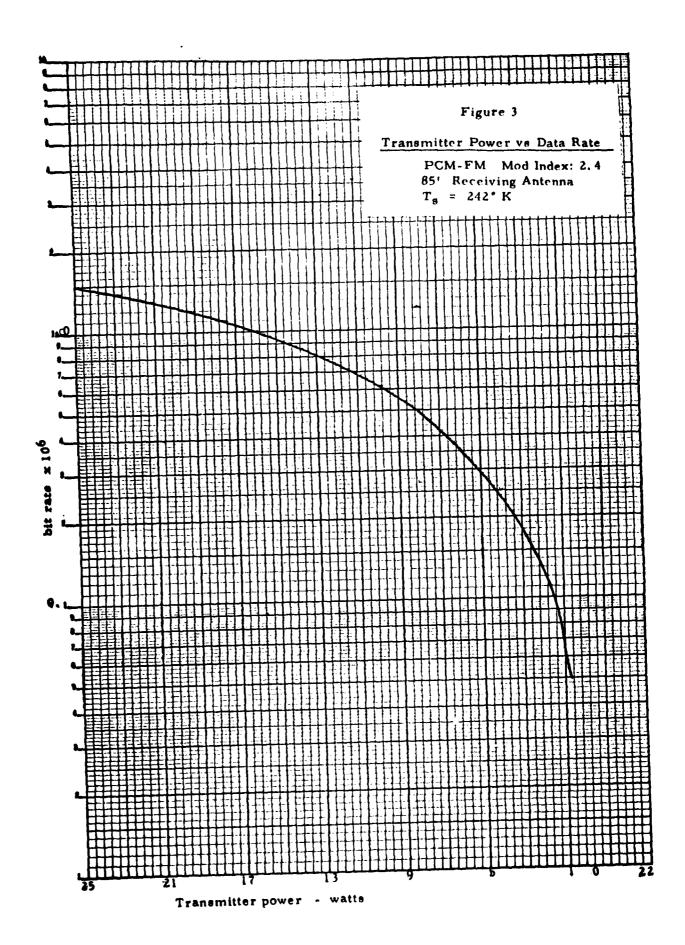
Modulation Index of 2. 4

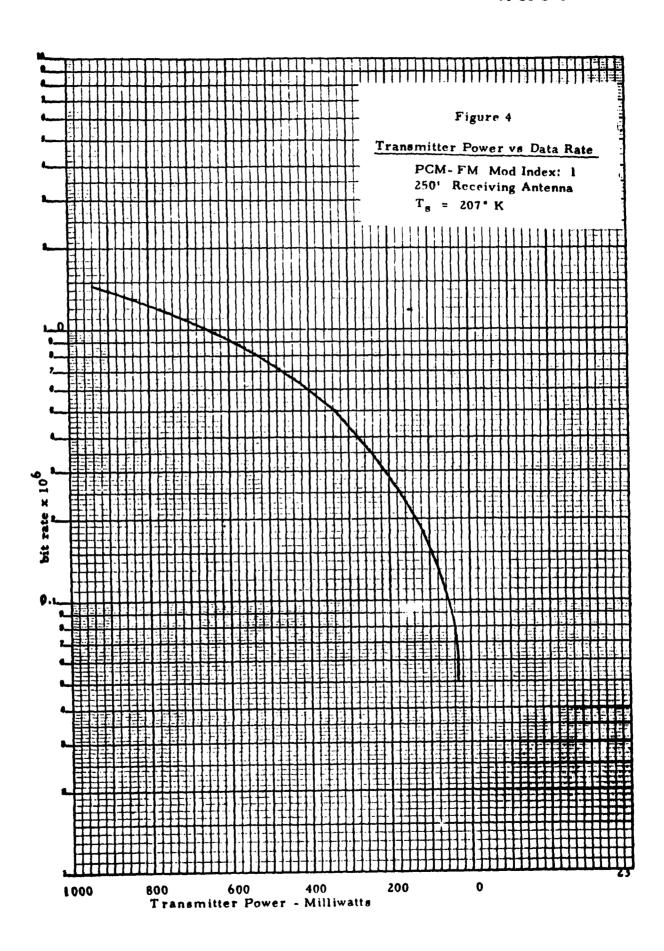
							91
Output S/N	(qp)	52	52	52	52	52	52
Transmitter Power (milli-	watts)	1680	1060	530	592	901	53
Transmi Power (mi	(dbw) (dbm)	32. 25	30. 25	27. 25	24. 25	20. 25	17. 25
	(dbw)	2. 25	0.25	-2. 75	-5.75	-9. 75	-12. 75
Net Trans- mission	(db)	128	1 28	1 28	128	128	128
Received Signal Power	PR (dbw)	-125.75	-127.75	-130.75	-133.75	-137.75	-140.75
	in B <u>if</u> (dbw)	-135.75	-137.75	-140.75	-143.75	-147.75	-150.75
I. F. Band-	width Bif	10. 2 mc	6.8 mc	3. 4 mc	1.7 mc	680 kc	340 kc
Peak	Deviation ΔF	3.6 тс		1, 2 mc	600 kc	240 kc	120 kc
Video Band -	width By	1.5 mc	1 mc	24 00 %	250 kc	100 kc	50 kc
Data	Rate bits/sec	1 5 × 106 1, 5 mc	901 - 1	501 - 3	2 5 4 105	1 - 105	5 x 104

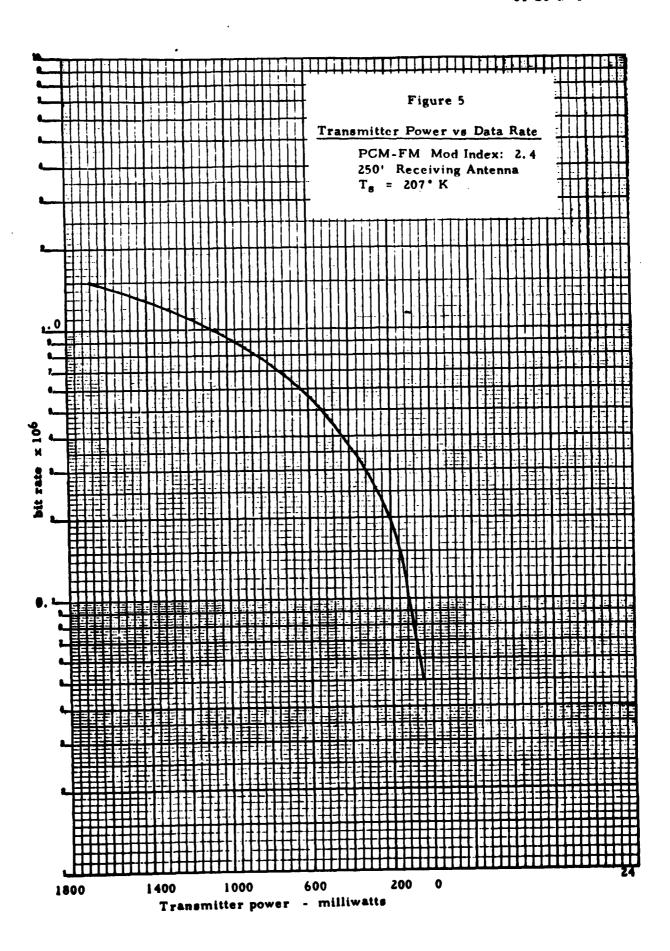
 $P_e << 10^{-7}$











COMMUNICATION REQUIREMENTS

REPORT No. 3

F. M.

Preliminary Transmitter RF Power Requirements

The purpose of this report is to determine the transmitter power requirements as a function of signalling rate for the Prospector moon-to-earth TV link.

The analysis that follows is based on a composite video signal frequency modulating (FM) an RF carrier.

The carrier frequency assumed is 2250 Mc and the ground-based receiver station will utilize the DSIF equipment.

Video Input

The video input signal to the communication transmitter will be derived from the output of the TV camera. The input signal will be a composite video containing both the video and synchronizer signals. The video signal will be in analog form and the synch signals will be in the form of pulses.

Video Output

The video output from the ground-based communication receiver will be a single-ended composite video signal.

System Parameters

Path distance moon-to-earth

2. 5 x 10⁵ statute miles

Carrier frequency

2250 Mc

Noise temperature T _g of moon ⁽¹⁾	130°X
Diameter of receiving antenna (2)	85 ft
Gain of receiving antenna (2), G	50 db
Noise temperature, T _r , (2) receiving antenna	50° K
Receiving antenna feed and coupling losses L	0.4 db
Low noise maser amplifier effective temperature, Te	30° K
Transmitting antenna dia. (parabolic)	4 ft
Transmitting antenna gain, G _t , based on 55% efficiency	27 db
Transmitter/antenna coupling and matching losses (assumed),	
$\mathbf{L_t}$	0.6 db
Circular polarization losses, Lp	3 db

Output S/N

In order to make a fair comparison between FM, PCM-PS and PCM-FM, equal video output S/N ratios will be assumed. In the PCM-PS and PCM-FM cases (see reports 1 and 2) 8 levels of gray were assumed requiring therefore 3 binary bits. The peak-to-peak signal to rms noise voltage therefore was

$$S/N = 2 \sqrt{3} S \tag{1}$$

where S = the number of quantum steps

so we obtaine

$$S/N = 2\sqrt{3} 8 = 27.7$$
 say $30:1 = 30$ db.

For the purpose of analysis in the FM case, let us assume a composite block negative video signal with a peak-to-peak white voltage $V_{pp} = 1$ and black level = 0.25 V_{pp} .

The output S/N therefore taking into account the synch pulses

$$=\frac{30}{75}$$
 = 40:1 = 32 db.

Analysis

The output S/N (rms signal) in an FM system is given by (5)

$$8/N = 10 \log_{10} \frac{P_R}{P_N} + 20 \log \left(\frac{\Delta F}{B_V} \right) + 10 \log \left(\frac{B_{1F}}{2B_V} \right) + 2 db$$
 (2)

The peak-to-peak signal/rms noise ratio is therefore

$$S_{PP}/N = 10 \log \frac{P_R}{P_N} + 20 \log \left(\frac{\Delta F^1}{B_V}\right) + 10 \log \left(\frac{B_{1F}}{2B_V}\right) + 2$$
 (3)

where P_R = the received signal power P_N = the noise power in the IF amplifier $\Delta F^1 = 2\Delta F$ = twice the peak deviation of the carrier P_{1F} = the IF bandwidth P_{1F} = the video bandwidth

2 db represents the difference between the 5 db triangular noise spectrum gain and -3 db limiter efficiency factor.

The results of the analysis are tabulated on Tables I through IV and plotted in Figures 1 through 4.

TABLE I TRANSMITTER POWER VS SIGNALLING RATE

FM, MOD IND EX: 1 85' RECEIVING ANTENNA T = 242'K

Signalling Rate (Elements/	Video Band- width	Peak Deviation	I F Band- width	Noise Power P _N , in	Recyd Signal Power	Net Trans- mission	Transmitter Power	itter	Output* S/N
() %	m ^{>}	40	an o	B.	(dbw)	(g)	(dpm)	(watts)	(qp)
5×10 ⁵	250 Kc	250 Kc	1 M c	-145	-124	139	15	31.6	32
2.5×10 ⁵	125 Kc	125 Kc	500 Kc	-148	-127	139	12	15.8	32
1x10 ⁵	50 Kc	50 Kc	200 Kc	-152	-131	139	co	6.3	32
5x104	25 Kc	25 Kc	100 Kc	-155	-134	139	۱n	3.15	32
1×104	5 Kc	5 Kc	20 Kc	-162	-141	139	7-	0.63	32

*Peak-to-peak signal/rms noise

T = System Noise Temperature

TABLE II

TRANSMITTER POWER VS SIGNALLING RATE

FM, MOD INDEX: 1 250' Receiving Antenna

T. = 207*K

Signalling Rate (Elements/	Video Bandwidth B	Peak Deviation $\Delta \mathbf{r}$	IF Band- width B _{IF}	Noise Power in B ₁ F P N (dbw)	Recyd Signal Power PR (dbw)	Net Trans- mission Loss (db)	Transi Po (dbw)	mitter wer (dbm)	(ma)	Transmitter Output* Power S/N (dbw) (dbm) (mw) (db)
5×10 ⁵	250 Kc	250 Kc	1 Mc	-145.7	-145.7 -124.7 128	128	3,3	33.3 2140 32	2140	32
2.5×10 ⁵	125 Kc	125 Kc	500 Kc	-148.7	-127.7 128	128	6.3	36.3	1070	32
1x10 ⁵	50 Kc	50 Kc	200 Kc	-152.7	-152.7 -131.7 128	128	-3.7	26.3	428	32
5x104	25 Kc	25 Kc	100 Kc	-155.7	-155.7 -134.7 128	128	-6.7	23.3	514	32
1×104	5 Kc	3	20 Kc	-162.7	-162.7 -141.7 128	·	-13.7	16.3	\$	35

* Peak-to-peak signal/ rms noise
T = System Noise Temperature

TABLE III TRANSMITER POWER VS SIGNALLING RATE

FM, MOD INDEX: 2.4 85' Receiving Antenna T₈ = 242°K

Signalling Rate (Elements/	Video Band- width	Peak Deviation	IF Band- width	Noise Power in B _{IF}	Recyd Signal Power	Net Trans- mission	Transmitter Power	itter	Output* \$/N
Sec)	m [▶]	V		of (gbg)	PR (dbw)	(db)	(dpm)	(dbw) (watts) (db)	(qp)
5x10 ⁵	250 Kc 600	600 Kc	1.7 Mc	-142.7	-131.6	139	7.4	5.5	32
2. 5x10 ⁵	125 Kc	300 Kc	850 Kc	-145.7	-134.6	139	4.4	2.75	32
1x10 ⁵	50 Kc	, 120 Kc	340 Kc	-149.7	-138.6	139	0.4	1.1	32
\$×104	25 Kc	60 Kc	170 Kc	-152.7	-141.6	139	-2.6	. 55	32
12104	5 Kc	12 Kc	34 Kc	-159.7	-148.6	139	-9.6	0.11	32

*Peak-to-peak Signal/rms Noise

T = System Noise Temperature

TABLE IV TRANSMITTER POWER VS SIGNALLING RATE

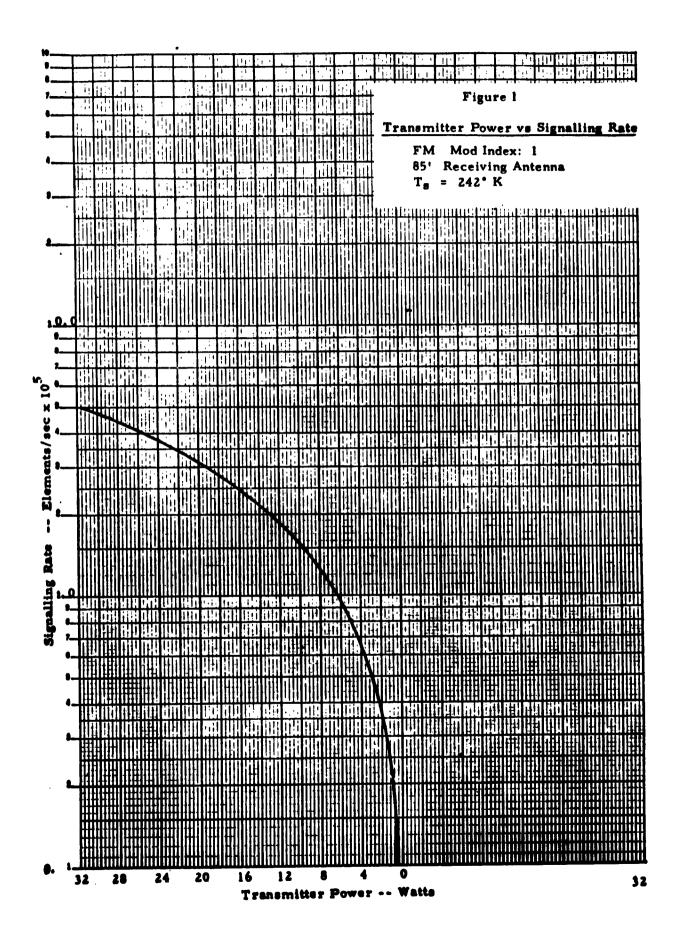
FIX, MOD INDEX: 2.4 250' Receiving Antenna

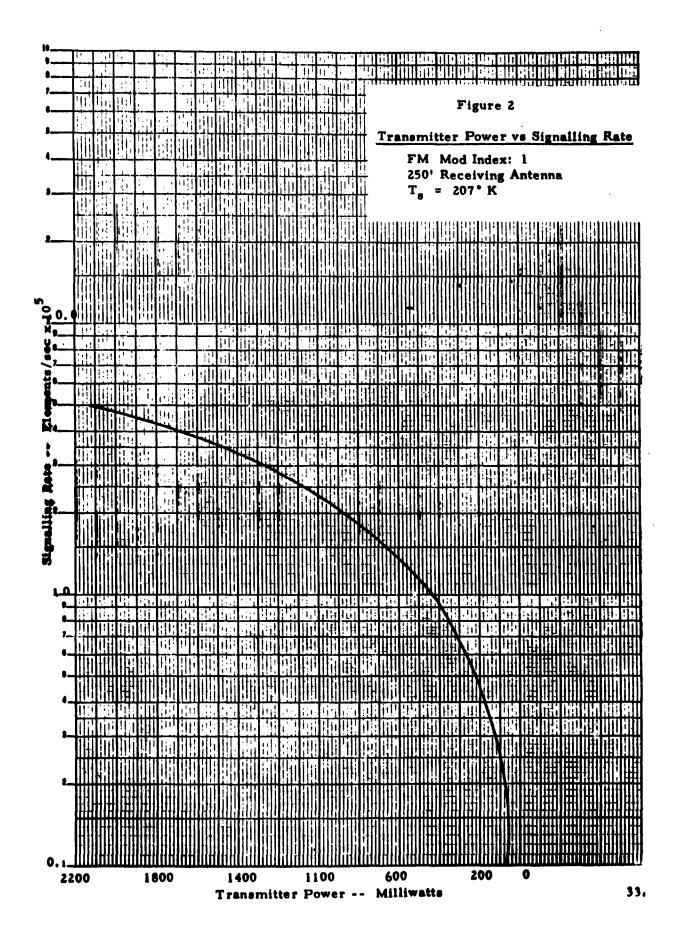
	(antat)	
	tter (dbm)	
	Transmitter Power (dbw) (dbm) (mw)	
	Net Trans- mission Loss (db)	
	Recyd Signal Power PR (dbw)	
7.K	Moise Power in B ₁ F P _N (dbw)	
T = 207 *K	IF Band - width B _{IF}	
	Peak Deviation	
	Video Band- width B	
	Signalling Rate (Elements/	

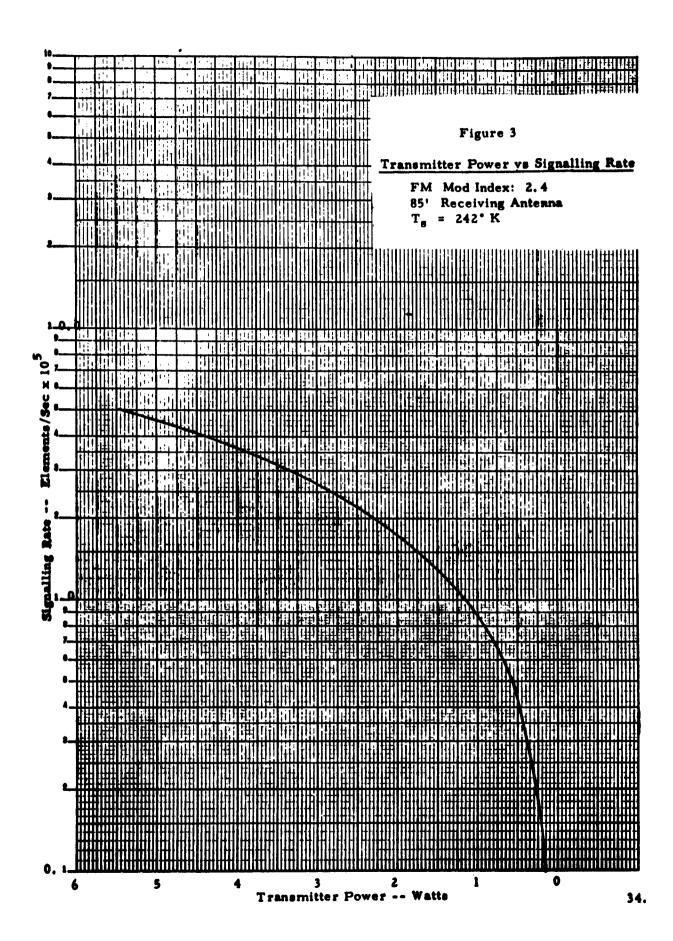
Output* S/N (db)

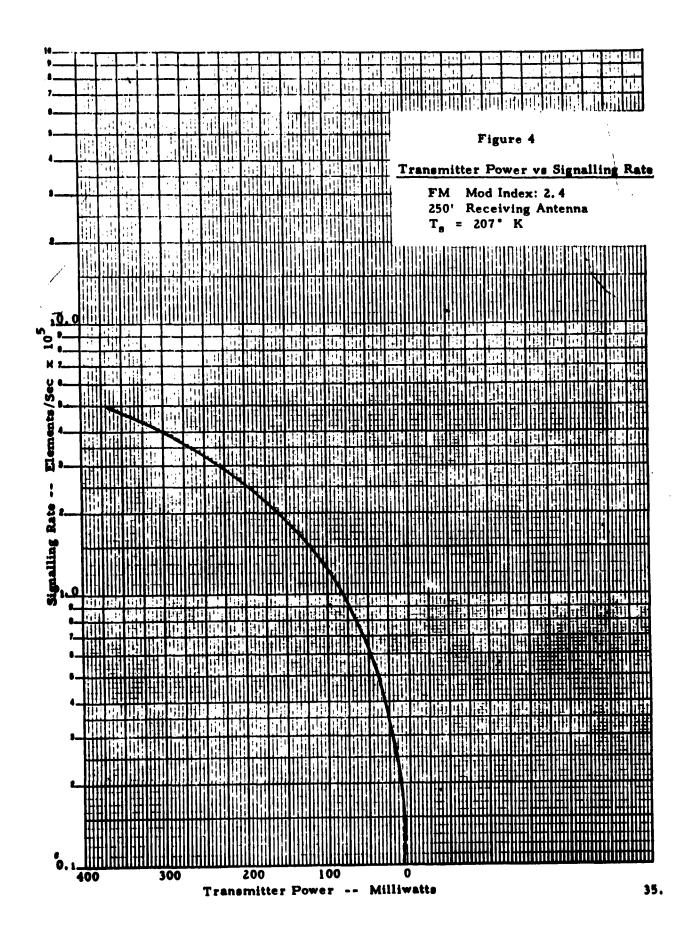
370 32	185 32	74 32	37 32	7.4 32
25.7	7.22	18.7 74	15.7	8.7
- 4.3 25.7	- 7.5	-11.3	-14.3	-21.3
128	128	128	128	128
-132.3	-135.3	-139.3	-142.3	-149.3
-143.4	-146.4	-150.4	-153.4	-160.4
1.7 Mc	850 Kc	340 Kc	170 Kc	34 Kc
600 Kc	300 Kc	120 Kc	60 Kc	12 Kc
280 Kc	125 Ke	8	28 80	2 %
501	2 K-105	2. 3410 3. 10.5	9 TX T	1x10

*Peak-to-peak Signal/rms noise T * System Noise Temperature









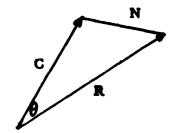
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APPENDIX I

S/N Ratio in an FM System

Assume (1) a carrier with a peak amplitude G (unmodulated), and angular velocity w; and (2) a noise component of peak amplitude N with a momentary angular velocity p. This leads to the summation of the two rotating vectors Ge-jwt and Nejpt. Now the resultant phase angle can be taken and wt subtracted from it to get the noise contribution to phase angle, or θ can be evaluated directly from the diagram.



The first case becomes:

$$Y = \tan^{-1} \frac{\sin wt + x \sin pt}{\cos wt + x \cos pt}$$
 (1)

where $x = \frac{N}{C}$

of
$$\theta = \tan^{-1} \frac{x \sin(p-w)t}{1+x \cos(p-w)t}$$
 (2)

In either case the expression

$$fd = \frac{1}{2\pi} \frac{d}{dt} (\theta \text{ or } \Psi)$$
 (3)

can be used for the contribution of the noise:

fd =
$$\left[\frac{1}{2w} (p-w) + (p-w) \frac{\frac{N}{C}^2 + \frac{N}{C} \cos(p-w)^t}{1 + \frac{N}{C}^2 + 2\frac{N}{C} \cos(p-w)^t}\right]$$
 (4)

The first term in the square bracket represents a direct current which can be ignored. The second term may be calculated to give:

$$\frac{1}{2\pi} \left\{ (p-w) \left[\left(\frac{N}{C} \right)^{2} - \left(\frac{N}{C} \right)^{4} + \left(\frac{N}{C} \right)^{6} - \left(\frac{N}{C} \right)^{8} - \dots \right] \right.$$

$$+ (p-w) \cos (p-w)^{4} \left[\left(\frac{N}{C} \right) - 3\left(\frac{N}{C} \right)^{3} + 5\left(\frac{N}{C} \right)^{5} - 7\left(\frac{N}{C} \right)^{7} + 9\left(\frac{N}{C} \right)^{9} - \dots \right]$$

$$- (p-w) \cos^{2}(p-w)^{4} \left[2\left(\frac{N}{C} \right)^{2} - 8\left(\frac{N}{C} \right)^{4} + 18\left(\frac{N}{C} \right)^{6} - 32\left(\frac{N}{C} \right)^{8} + 50\left(\frac{N}{C} \right)^{10} - \dots \right]$$

$$+ (p-w) \cos^{3}(p-w)^{4} \left[4\left(\frac{N}{C} \right)^{3} - 20\left(\frac{N}{C} \right)^{5} + 56\left(\frac{N}{C} \right)^{7} - 120\left(\frac{N}{C} \right)^{9} + 220\left(\frac{N}{C} \right)^{11} - \dots \right]$$

$$- (p-w) \cos^{4}(p-w)^{4} \left[8\left(\frac{N}{C} \right)^{4} - 48\left(\frac{N}{C} \right)^{6} + 104\left(\frac{N}{C} \right)^{8} - 224\left(\frac{N}{C} \right)^{10} + \dots - \dots \right]$$

$$+ (p-w) \cos^{5}(p-w)^{4} \left[16\left(\frac{N}{C} \right)^{5} - 64\left(\frac{N}{C} \right)^{7} + 168\left(\frac{N}{C} \right)^{9} - \dots - \dots - \dots \right]$$

$$- (p-w) \cos^{6}(p-w)^{4} \left[32\left(\frac{N}{C} \right)^{6} - 160\left(\frac{N}{C} \right)^{8} + 328\left(\frac{N}{C} \right)^{10} - \dots - \dots - \dots - \dots - \dots \right]$$

$$- (p-w) \cos^{7}(p-w)^{4} \left[64\left(\frac{N}{C} \right)^{7} - \dots - \dots \right]$$

$$- (p-w) \cos^{7}(p-w)^{4} \left[64\left(\frac{N}{C} \right)^{7} - \dots - \dots \right]$$

$$- (p-w) \cos^{7}(p-w)^{4} \left[64\left(\frac{N}{C} \right)^{7} - \dots - \dots \right]$$

The first terms give added direct current due to the difference frequency. The main term, if N/C is small, is

$$\frac{N}{C}$$
 (p-w) cos (p-w)t

which shows that a noise component gives an output proportional to N/C and proportional to its spacing from the carrier frequency.

Now consider an i-f amplifier in which a signal-to-thermal noise power ratio of C/N has been calculated. Then by taking an interfering signal at a frequency f from the carrier (considering it one noise component), the power will be n = N/Bif. The ratio of amplitude

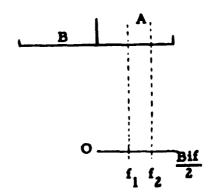
$$=\sqrt{\frac{n}{C}}$$

From the analysis above, the interfering carrier will produce an output of

$$K\sqrt{\frac{n}{C}f}$$

where K is the demodulator transfer constant. Now if the frequency of the interfering carrier is varied throughout the i-f band, we find that an output is produced between fl and f2 when the carrier is in the A region and also when it is in the B region. The power per cycle in the fl to f2 range from the multiplicity of carriers comprising the noise in the A region is

$$= \kappa^2 \frac{n}{C} f^2$$



The noise power appearing in band fl to f2 is:

$$2 K^{2} \frac{n}{C} \int_{1}^{f_{2}} f^{2} df = 2 K^{2} \frac{n}{C} \frac{1}{3} (f_{2}^{3} - f_{1}^{3})$$
 (8)

where 2 takes care of both A and B regions.

The signal in the output will be $K \triangle F$ in amplitude, or $K^2 \triangle F^2$ in power, so the output signal to noise ratio will be:

$$\frac{K^{2} (\Delta F)^{2} 3}{2 K^{2} (f_{2}^{3} - f_{1}^{3})} \frac{C}{n} = \frac{C}{N} \frac{Bif}{2 (f_{2} - f_{1})} \frac{3 (\Delta F)^{2}}{(f_{2}^{2} + f_{1}^{2} f_{2} + f^{2})}$$
(9)

Summary

$$S/N (rms) = \frac{C}{N} \frac{Bif}{2(f_2 - f_1)} \frac{3(\Delta F^2)}{(f_2^2 + f_1 f_2 + f^2)}$$
 (0)

Since in a wide band modulation system $f_2 >> f_1$,

$$S/N \text{ (rms)} = \frac{C}{N} = \frac{Bif}{2(f_2 - f_1)} = \frac{3(\Delta F^2)}{(f_2^2)}$$
 (11)

If we let $f_2 - f_1 = Bv$ the video bandwidth, and $f_2 = f_t$ the highest video frequency,

$$S/N (rms) = \frac{C}{N} \frac{Bif}{2(B_v)} 3 \left(\frac{\Delta F}{f_t}\right)^2$$
 (12)

To convert to db we multiply each side of Equation (12) by $10 \log_{10}$ to obtain:

$$8/N \ db = 10 \log_{10} \frac{C}{N} + 10 \log_{10} \frac{Bif}{2 B_v} + 5 \ db + 20 \log_{10} \frac{\Delta F}{f_t}$$
 (13)

Equation (13) assumes perfect limiting, if we assume a limiter efficiency of 50%. Equation (13) then becomes

$$8/N = 10 \log_{10} \frac{C}{N} + 10 \log_{10} \frac{Bif}{2B_v} + 20 \log_{10} \left(\frac{\Delta F}{f_t}\right) + 5-3 db$$
 (14)